A student in 1120 emailed me to ask how much extra he should expect to pay on his electric bill when he strings up a standard 1-strand box of icicle holiday lights outside his house. (total, cumulative cost)? Try to make a real estimate, don't just guess! Energy in Colorado costs about 10¢/kW hr.

A: Less than 1 cent

B: Between 1 cent and 10 cents

- C: Between \$.10 and \$1.00 D: Between \$1.00 and \$10.00
- E: More than \$10.00

50-100 Watts? (Like ONE bulb). 12 hrs/day? 30 days? ~100 W * 10 hrs/day * 30 days = 30,000 W*hrs = 30 kW hrs. ⇒\$3 (for 100 million Joules! Energy is cheap...)

Welcome back!!

CAPA #13 is due Friday New online participation survey is up! Pretest tonight (and Tut hw for tomorrow)

Reading: catch up if you're behind! E.g. 35.6 (1st 2 pp) (We'll finish up Ch. 33 this week -all sections, including 33.6)

Last: Transformers and Induction Today: Inductors in circuits Next: AC circuits

Inductor = (coil of wire)

Important fact: Magnetic Flux $\Phi_{\rm B}$ is proportional to the current making the $\Phi_{\rm B}$

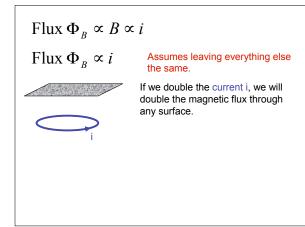
All our equations for B-fields show that B α i

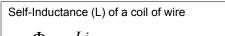
$$d\bar{B} = \frac{\mu_0 i}{4\pi} \frac{d\bar{l} \times \hat{r}}{r^2}$$

Biot-Savart

Ampere

 $\oint \vec{B} \cdot d\vec{l} = \mu_0 i_{thru}$





$$\Phi_B = Li$$

$$L = \frac{\Phi_B}{\Delta B}$$

i

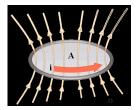
This equation defines self-inductance.

Note that since $\Phi_{B}\,\alpha$ i, L must be independent of the current i.

L has units [L] = [Tesla meter²]/[Amperes] New unit for inductance = [Henry].



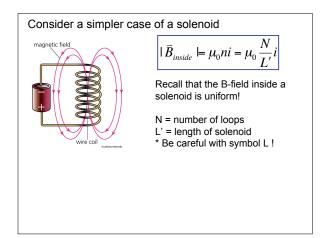
An inductor is just a coil of wire.

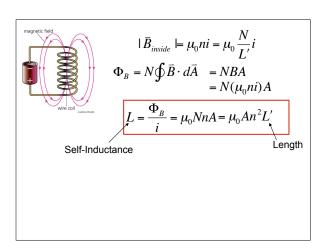


The Magnetic Flux created by the coil, through the coil itself:

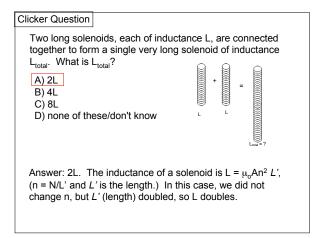
 $\Phi_{\scriptscriptstyle B}=\oint \vec{B}\cdot d\vec{A}$

This is quite hard to calculate for a single loop. Earlier we calculated B at the center, but it varies over the area.





Inductor 1 consists of a single loop of wire. Inductor 2 is identical to 1 except it has two loops on top of each other. How do the self-inductances of the two loops compare? A) $L_2 = 2 L_1$ B) $L_2 > 2L_1$ C) $L_2 < 2L_1$ A) $L_2 = 2 L_1$ B) $L_2 > 2L_1$ C) $L_2 < 2L_1$ HINT 1: What is the B field at the center of coil 2, B2, compared to the field in the center of coil 1? HINT 2: inductance L = $\Phi(\text{Iotal})/I$ Answer: L2 > 2L1, in fact L2 is roughly 4 L1! Recall L = Φ/I . When N doubles => B doubles. $\Phi(\text{each loop})$ doubles (because *B is doubled*) But $\Phi(\text{tot}) = 2 \Phi(\text{each loop})$, so double*double = 4 times!



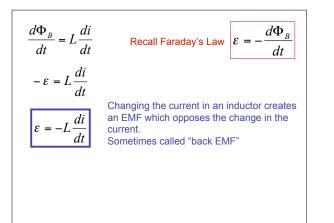


What does inductance tell us?

$$L = \frac{\Phi_B}{i}$$
$$\Phi_B = Li$$

-

 $\frac{d\Phi_{B}}{dt} = L\frac{di}{dt}$ L is independent of time. Depends only on geometry of inductor (like capacitance).



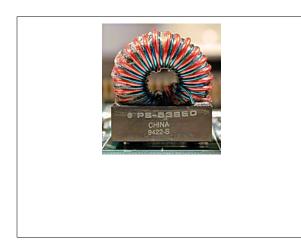


$$\varepsilon = -L\frac{di}{dt}$$

It is difficult (requires big external Voltage) to change quickly the current in an inductor.

The current in an inductor **<u>cannot</u>** change instantly.

If it did (or tried to), there would be an infinite back EMF. This infinite back EMF would be fighting the change!

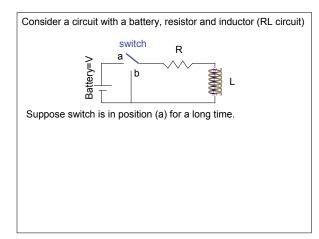


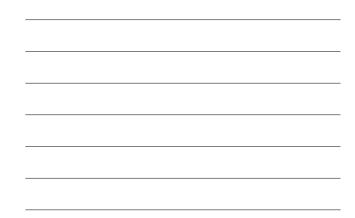
What do these inductors do in circuits?

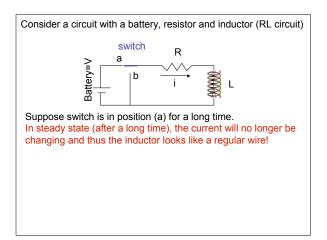
Just recall that the EMF or Voltage across an inductor is:

$$\varepsilon = -L\frac{di}{dt}$$

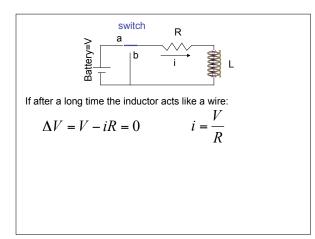
So, when we add them to circuits, we can apply the usual Kirchhoff's Voltage Law and include the inductors.

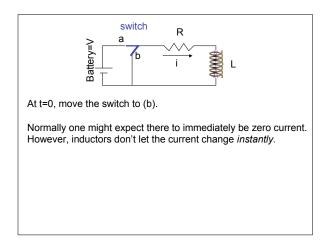




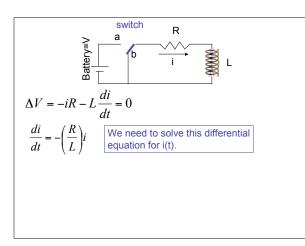














$$\frac{di}{dt} = -\left(\frac{R}{L}\right)i$$

$$i(t) = i_0 e^{-\left(\frac{R}{L}\right)t} \quad \text{where} \quad i_0 = \frac{V}{R}$$

$$i(t) = i_0 e^{-t/\left(\frac{L}{R}\right)} \quad \text{Current exponentially decays with}$$

$$\text{Time Constant} = \tau = L/R \text{ (units of seconds).}$$

