

Chapter 28 Direct Current Circuits

The discussion is restricted to direct currents (dc) that flows only in one direction. We first study a steady state case and then go on to a time-varying condition.

When a current flows through a resistor, electrical energy is dissipated. A circuit cannot consist solely of **passive devices**; there must also be some source of electrical energy (**active devices**). Such a device is called a source of **electromotive force**, abbreviated **emf**.



Why don't we use a direct current circuit to transmit electric power? (extra bonus)

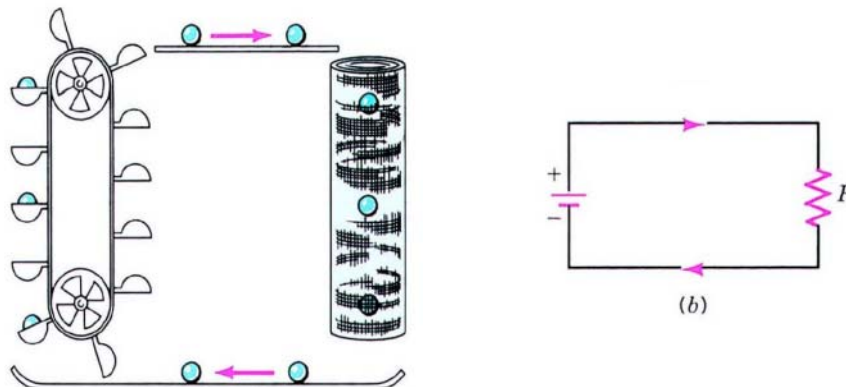
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28.1 Electromotive Force

An emf is the work per unit charge done by the source of emf in moving the charge around a *closed loop*.

$$\mathcal{E} = \frac{W_{ne}}{q}$$

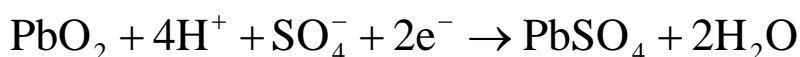
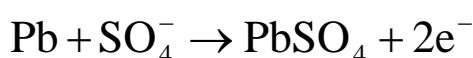
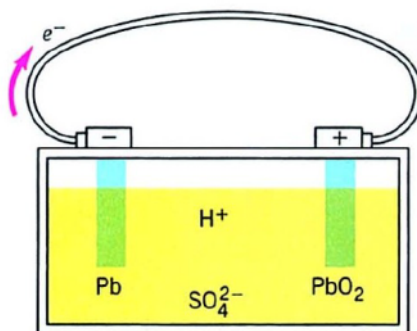
The subscript "ne" emphasizes that the work is done by some nonelectrostatic agent, such as a battery or an electrical generator.



What is the difference between emf and potential difference?

28.1 Electromotive Force: Production of a current

What is the function of the acid solution in the voltaic pile?



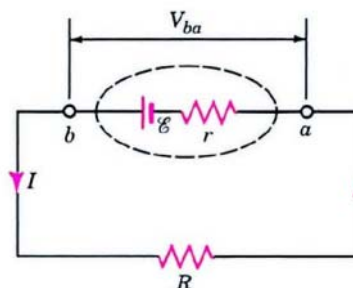
Note that for every electron that leaves the Pb plate, another enters the PbO₂ plate.

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28.1 Electromotive Force: Terminal Potential Difference

A real source of emf, such as a battery, has *internal resistance*.

$$V_{ba} = V_b - V_a = \mathbf{E} - Ir$$



The change in potential is called the **terminal potential difference**.

Unlike the emf, which is a fixed property of the source, the terminal potential difference depends on the current flowing through it.

As a battery ages its internal resistance increases, and so, for a given output current, the terminal potential difference falls.

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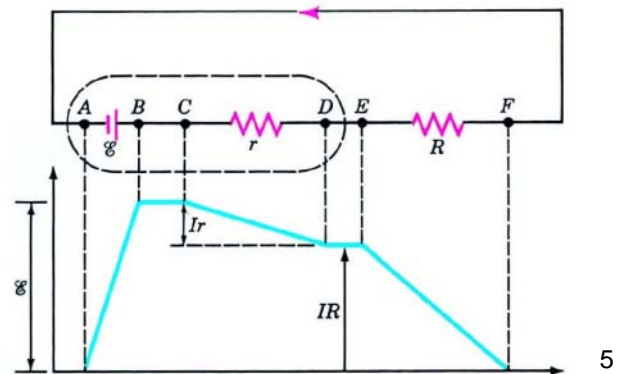
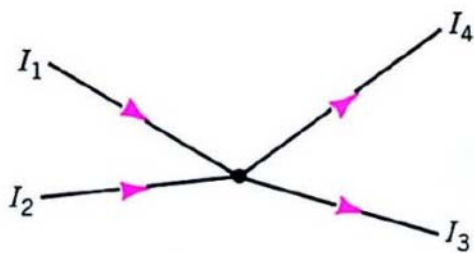
28.2 Kirchhoff's Rules

Kirchhoff's junction rule: the conservation of charge

The algebraic sum of the currents enter or leaving a junction is zero. $\Sigma I=0$

Kirchhoff's loop rule: the conservation of energy

The algebraic sum of the changes in potential around a closed loop is zero. $\Sigma V=0$



28.3 Series and Parallel Connection

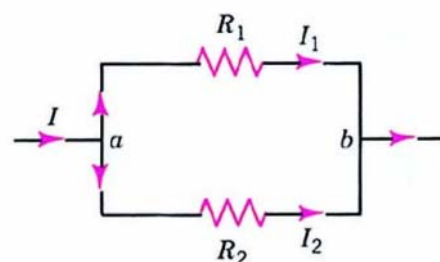
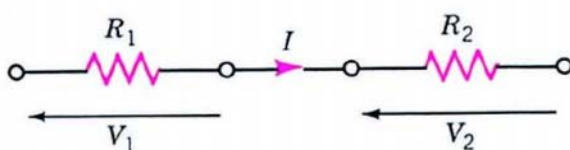
Resistors, like capacitors, can be connected in series and in parallel.

(Series)

$$R_{eq} = R_1 + R_2 + R_3 + \dots + R_N$$

(Parallel)

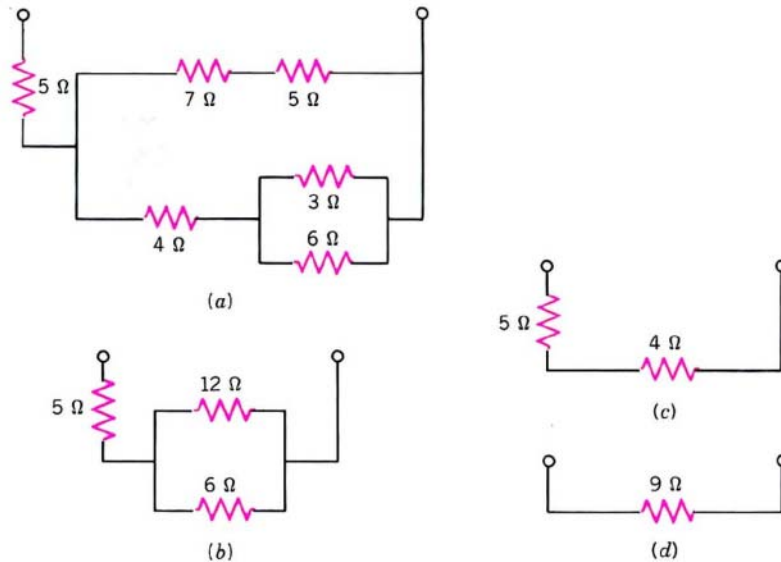
$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots + \frac{1}{R_N}$$



Example 28.1

Find the equivalent resistance of the combination of resistors shown in Fig. 28.10a.

Solution:



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Example 28.3

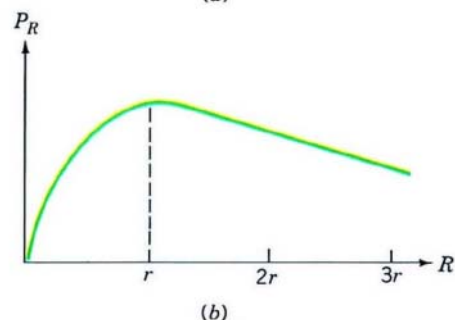
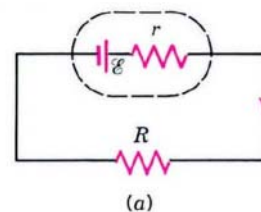
Whenever a real source of emf supplies power to an external load, some power is also dissipated in the internal resistance. A load resistance R is connected to a source of emf whose internal resistance is r , as in Fig. 28.11a. For what value of R will the power supplied to the load be a maximum?

Solution:

$$P = I^2 R = \frac{\mathcal{E}^2 R}{(R + r)^2}$$

$$\frac{dP}{dR} = \mathcal{E}^2 \left(\frac{1}{(R + r)^2} - \frac{2R}{(R + r)^3} \right)$$

$$\frac{dP}{dR} = 0 \Rightarrow R = r$$



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Example 28.5

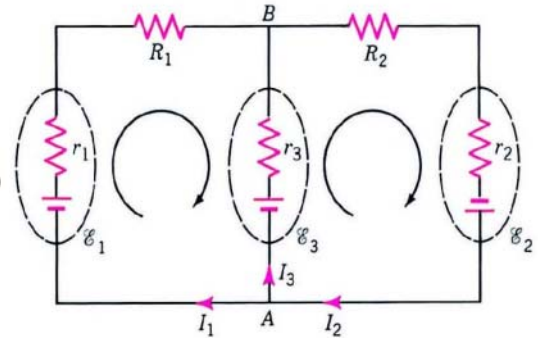
The circuit in Fig. 28.14 has two loops and three sources of emf. (a) determine the currents given that $r_1=r_2=2$ ohm, $r_3=1$ ohm, $R_1=4$ ohm, $R_2=4$ ohm, $\mathcal{E}_1=15V$, $\mathcal{E}_2=6V$, and $\mathcal{E}_3=4V$. (b) What is the change in potential V_a-V_b ?

Solution:

Left loop $15 - 2I_1 - 4I_1 + I_3 - 4 = 0$

right loop $4 - I_3 - 3I_2 + 6 - 2I_2 = 0$

junction rule $I_1 - I_2 + I_3 = 0$



When analyzing a circuit, the currents may be drawn in arbitrary directions.

Example 28.6

Five resistors are connected as shown in Fig. 28.15. What is the equivalent resistance between points a and b?

Solution:

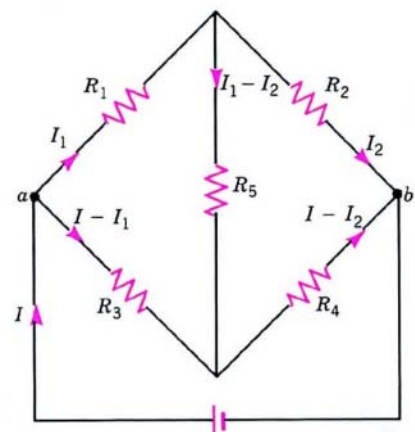
Applying the junction rules

Left loop $-I_1R_1 - (I_1 - I_2)R_5 + (I - I_1)R_3 = 0$

right loop $+(I_1 - I_2)R_5 - I_2R_2 + (I - I_2)R_4 = 0$

$I_1 = \alpha_1 I, \quad I_2 = \alpha_2 I$

$V_b - V_a = -I_1R_1 - I_2R_2 = -(\alpha_1R_1 + \alpha_2R_2)I$

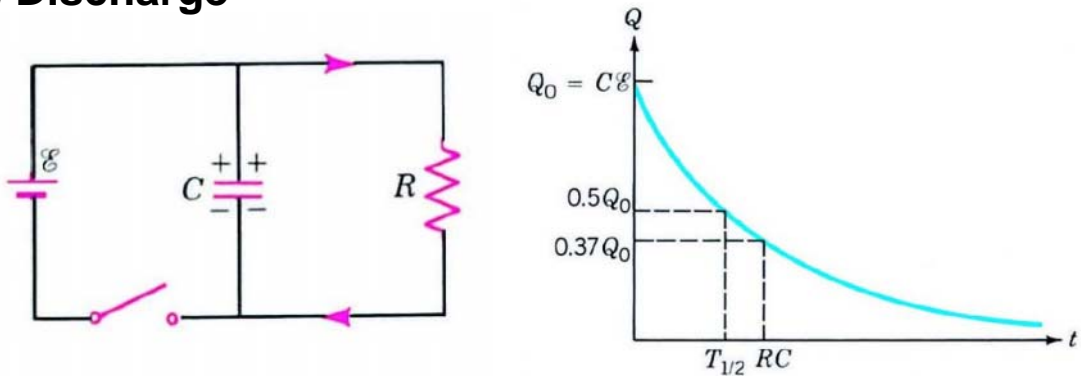


28.4 RC Circuits: Charge and Discharge

When a capacitor is connected directly across the terminals of an ideal battery, the capacitor becomes **charges** instantaneously.

Similarly, if the terminals of a charges capacitor are connected by a wire, the capacitor is **discharged** instantaneously.

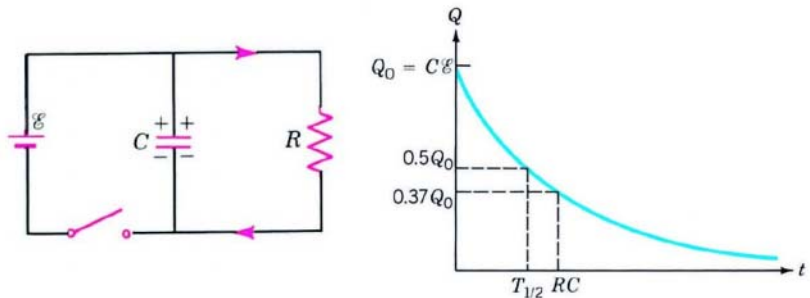
(i) Discharge



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28.4 RC Circuits: Charge and Discharge

(i) Discharge



loop rule $\frac{Q}{C} - IR = 0$

The current I is equal to the rate at which the charge Q is decreasing; therefore, $I = -dQ/dt$, the loop rule becomes

$$\frac{dQ}{dt} = -\frac{Q}{RC} \Rightarrow Q = Q_0 e^{-t/RC}$$

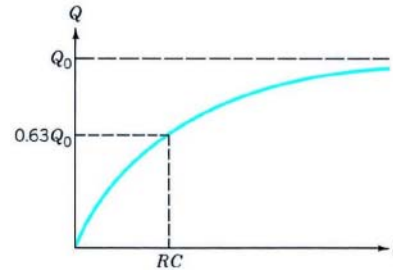
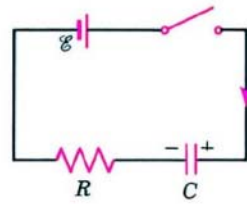
time constant $\tau = RC$ when $Q = Q_0 e^{-1}$

half - time $T_{1/2} = RC \ln 2$ when $Q = \frac{1}{2} Q_0$

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28.4 RC Circuits: Charge and Discharge

(ii) Charge



$$\text{loop rule} \quad \varepsilon - IR - \frac{Q}{C} = 0$$

In this circuit, the current I increases the charge on the capacitor, and therefore, $I = +dQ/dt$, the loop rule becomes

$$C\varepsilon - Q = \frac{dQ}{dt} RC \quad \Rightarrow \quad Q = Q_0(1 - e^{-t/RC})$$

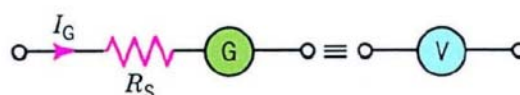
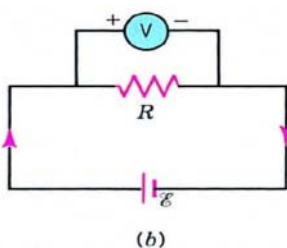
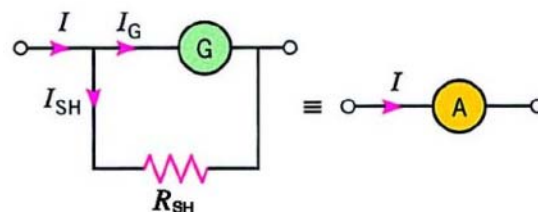
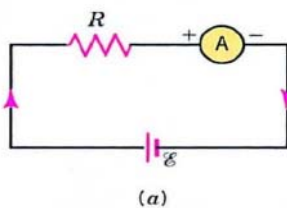
$$I = I_0 e^{-t/RC}$$

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28.5 Direct Current Instruments

An instrument that measures current is called an **ammeter**, and one that measures potential difference is called a **voltmeter**. Many of these meters are based on the **galvanometer**. An **ohmmeter** is an instrument designed to measure resistance.

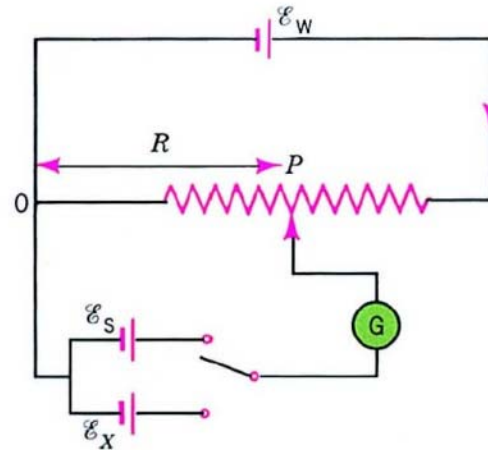
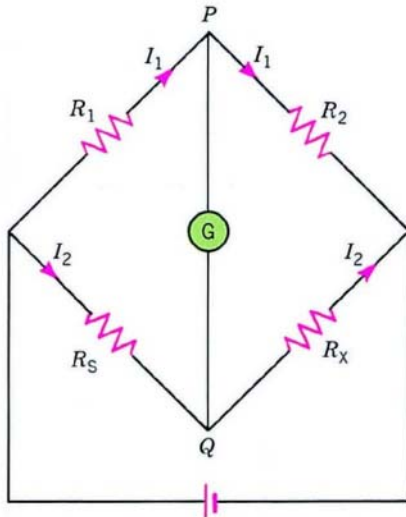
A commercial meter, which uses to measure current, voltage, resistance, and capacitance, is called **multimeter**.



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28.5 Direct Current Instruments (II)

Wheatstone Bridge & Potentiometer



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Exercises and Problems

Ch.28:

Ex. 25, 42

Prob. 1, 2, 4, 7, 12, 13, 15

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